# POSSIBLE CORRELATION BETWEEN MIOCENE GLOBAL CLIMATIC CHANGES AND <br> MAGNETIC PROXIES, USING NEURO FUZZY LOGIC ANALYSIS IN A STRATIGRAPHIC WELL AT THE LLANOS FORELAND BASIN, COLOMBIA 

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#### Abstract

In this work we have assessed the hybrid algorithm of NeuroFuzzy logic (NFL), to establish a correlation between global climatic changes (benthic foraminiferal $\delta^{18} O$ data), experimental S-ratio (factor characterizing stability of remanent magnetization) and magnetic susceptibility ( $\kappa$ ). Magnetic proxies have been measured in 44 samples of the Colombian stratigraphic well Saltarin 1 (distal Llanos foreland basin). $\kappa$ and $S$ ratios were linked to global $\delta^{18} O$ data assuming a constant accumulation rate for a 305 meters thick stratigraphic interval flanked by the two palynological age constrains available. This interval encompasses, from top to base, the bottom of the Guayabo formation, the León, and the upper unit of the Carbonera formations (lower to middle Miocene). The best inference is accomplished applying a Takagi-Sugeno-Kan (TSK) fuzzy model with four fuzzy rules and the $\delta^{18} O, S$-ratios and $\kappa$ data used in a linear form to train the system. These results are interpreted as the outcome of a significant influence of global climatic changes upon magnetic proxies. A stronger correlation is perhaps prevented by the likely influence of local and regional tectonic events and climatic changes that could have affected the distal segment of the Colombian Llanos foreland basin during Miocene times. We argue that late diagenesis of primary magnetic minerals and the assumption of a constant accumulation rate might have a minor influence on these results.


Keywords: $\delta^{18} \mathrm{O}$, magnetic susceptibility, S-ratio, NeuroFuzzy logic

## 1. INTRODUCTION

The inference of a relationship, that would allow connecting data of different physical nature in order to characterize distinct systems, is a common practice in geosciences. Linear regression methods are applied to most of these cases in order to establish a possible correlation between the various parameters that are being used. However, the complexities involved in geological and geophysical problems give rise to an increasing dispersion of these data. In such situations, there is not an obvious trend that could be easily adjusted by a single linear or multilinear relationship. This problem has been partially solved in the prediction of permeability, out of porosity data, by dividing the set of experimental points in smaller subunits that correspond to different sedimentary facies, followed by the calculation of a local fitting function for each of these subunits (Finol et al., 2001).

The obvious limitations of the linear regression method, when applied to a set of highly scattered experimental data points, make it necessary to find alternative ways to deal with this kind of intricate problems. Some mathematical approaches apply concepts of neural networks and/or fuzzy logic to handle non-linear relationships between two or more variables (i.e. Helle et al., 2001 and Cuddy and Glover, 2001). In rock magnetism, Urbat et al. (1999) have used fuzzy c-means clustering and non-linear mapping in order to identify and characterize early diagenetic effects in large rock magnetic data sets of the Ocean Drilling Program (ODP) Site 904. Likewise, the NeuroFuzzy logic (NFL) method, a hybrid algorithm that combines fuzzy logic with neural networks, has been previously used in the prediction of complex petrophysical parameters (Hurtado et al., 2008). In most situations, the results obtained have given rise to a set of numerical connections between the different variables involved as well as additional lithological information about an area of particular interest (Finol et al., 2001 and Hurtado et al., 2008, among others).

In this work we employ, for the first time, the NFL hybrid method with the aim of establishing a correlation between magnetic parameters (i.e. $S$-ratio and/or initial magnetic susceptibility) and benthic foraminiferal $\delta^{18} \mathrm{O}$ data, as a finite series of flexible local models (Finol and Jing, 2002).

Benthic foraminiferal $\delta^{18} \mathrm{O}$ values have been taken from the deep-sea oxygen record, based on data compiled from more than 40 Deep Sea Drilling Program (DSDP) and ODP sites by Zachos et al. (2001). It is well known that these $\delta^{18} \mathrm{O}$ values are linked to the amount of global ice volume released into the oceans and, therefore, to sea level changes. However such major events are somewhat the response to global variations of temperature. Indeed, throughout glacial periods the polar ice sheets grow at expense of atmospheric waters enriched in lighter ${ }^{16} \mathrm{O}$ (low $\delta^{18} \mathrm{O}$ values). The result is a fall of the sea level and the enrichment of the ocean water in heavier ${ }^{18} \mathrm{O}$ (high $\delta^{18} \mathrm{O}$ values). Conversely, the dissolution of the ice sheets, during interglacial periods, reinstates the ocean to its initial conditions, namely a rise of the sea level and the decline of global benthic foraminiferal $\delta^{18} \mathrm{O}$ values. Thus, after the early Oligocene, most of the benthic foraminiferal $\delta^{18} \mathrm{O}$ values appear to mirror global climate changes by reflecting the variations in Antarctic (eastern and western ice sheets) and Northern Hemisphere ice volume released into the oceans.

On the other hand, $S$-ratio and initial magnetic susceptibility have been directly measured on samples from a 305 meters-thick sedimentary sequence that belongs to the stratigraphic well Saltarín 1A (distal Llanos foreland basin in Colombia).

The $S$-ratio is a rock magnetic index that accounts for the relative contributions of low and high coercivity minerals to the total saturation isothermal remanent magnetization in a sample. In this study, $S$-ratios have been obtained according to the definition by Bloemendal et al. (1992) and they reflect somehow the variability of redox conditions for different sedimentary environments along the stratigraphic column.

Initial magnetic susceptibility ( $\kappa$ ) in sedimentary rocks depends mainly on the concentration of ferrimagnetic minerals (e.g. Ti-magnetite). Since the pioneer works by Shackleton and Opdyke (1973) and Kent (1982), $\kappa$ has been widely used, in numerous studies on loess (e.g. Zhu et al., 2001; Retallack et al., 2003; Balsam and Chen, 2004), lake (e.g. Geiss and Banerjee, 1997; Hu et al., 2000) and marine sediments (Alexander et al., 1993; Brachfeld and Banerjee, 2000; Moreno et al., 2002), as a magnetic proxy that reflects global climate cycles.

Kent (1982) has also pointed out that magnetic parameters (i.e. $\kappa, N R M$ and/or IRM), measured in deep sea sediments, seem to mirror the variability of carbonate content in these rocks. In turn, such lithological features appear to be finely tuned with global climate changes over long geological time periods. Hilgen (1991) has associated recurring sedimentation, also controlled by carbonate content across five sapropel sections in southern Italy and Greece, to a cyclic pattern of insolation intervals deduced from the astronomical calculations by Laskar (1990). This pattern echoes the position of the Earth's rotational axis and orbital path (Milankovich cycles). Orbital age calibration has been also applied, in connection with magnetic susceptibility, to obtain a high-resolution astrochronological timescale (e.g. Heller and Liu, 1986; Williams et al., 1997; Lu et al., 1999; Heslop et al., 1999 and Heslop et al., 2000).

In less global terms, past climate variations at low (near equatorial) latitudes are not well understood, mostly because the scarcity of continental tropical sites in which mean annual temperatures (MAT) can be determined. The Llanos foreland basin in eastern Colombia, where the stratigraphic well Saltarín 1A is located, evolved in this kind of geographical setting. The last major episode of large-scale warming was the Middle Miocene Climatic Optimum which lasted for about 2-3 Ma (14 to 17 Ma ), and took place during the long-term cooling of the Neogene (Zachos et al., 2001). One possible assumption is that global warming affected the continental Llanos foreland basin and surrounding areas. However, new research should be conducted to determine these MAT. The stratigraphic interval used for this study partly corresponds to this Middle Miocene Climatic Optimum.

The change from fluvial to lacustrine paleoenvironmental conditions in the Llanos foreland basin, during early and middle Miocene times, has been widely documented in previous works carried out on the Saltarín 1A and other nearby oil wells in Colombia and Venezuela (Bayona et al., 2007, 2008a,b, 2009). These studies also provide evidence for large-scale variations in tectonic subsidence and long-term changes in sediment supply rates. Such conditions, together with climate variations (i.e. Middle Miocene Climatic Optimum) obviously affected the sedimentary filling of a distal continental foreland basin (Bayona et al., 2007, 2008a,b, 2009). Thus, Saltarín 1A seems to be the ideal scenario to
asses the possibility of finding, via the NFL method, a relationship between magnetic proxies and global climate changes. Due to the complex geological history of the basin, we would expect that local and regional tectonics and climatic factors would have also had a considerable weight on the record contained by the magnetic proxies.

Several computational trials are required to check for the optimal set of empirical correlations between benthic foraminiferal $\delta^{18} \mathrm{O}$ data with $\kappa$ and $S$-ratios. If we build the NeuroFuzzy system using only benthic foraminiferal $\delta^{18} \mathrm{O}$ data and either $\kappa$ or $S$-ratios, we are taking for granted that there is a simple and unique relationship involving each pair of variables. However, $\kappa$ and $S$-ratios could have been independently affected, to a different extent, by local and regional tectonic events as well as by local and global climate changes (Harris and Mix, 2002). Moreover, late diagenesis of primary magnetic minerals probably had variable consequences on the magnetic parameters measured in these samples. Therefore, a better inference of $\delta^{18} \mathrm{O}$ data should be obtained by considering two mutually complementary magnetic proxies that are not related to each other by a simple univocal and linear way, namely $\kappa$ and $S$-ratio (Frank and Nowaczyk, 2008; Heslop, 2009).

Since the primary, or nearly primary, magnetic record in these rocks might be partially or completely obliterated by tardy alteration effects, it is essential to be cautious in interpreting magnetic variations as global paleoclimate proxies. Therefore, in order to monitor or preclude late digenesis events, we discuss some results of thermomagnetic susceptibility experiments (continuous heating and cooling cycles), scanning electron microscopy (SEM) and energy dispersive X-ray spectroscopy (EDX) analyses, obtained from magnetic separates of some selected samples.

## 2. SAMPLES AND METHODS

The $\kappa$ and $S$-ratios used in this study were measured for 44 samples from the Colombian stratigraphic well Saltarín 1A (Fig. 1). The samples, provided by Hocol S.A. (Bogotá, Colombia), were taken at approximately every 7 m , between stratigraphic levels 304.75 and 610.20 m (see Table 1). This is about the typical spacing between samples cored for petrophysical and conventional geological analyses (i.e. from 5 up to 15 m ).

The 305 m depth interval, where we have restricted our study, encompasses mainly the Guayabo formation lower units G1, G2 and G3 (15 samples), León formation ( 23 samples) and Carbonera formation upper sandstone unit C 1 ( 6 samples), as shown in Fig. 2.

Sedimentological, stratigraphic, biostratigraphic, and provenance analyses carried out in Saltarín 1A allowed the identification of major lithologies and the interpretation of sedimentary conditions for each stratigraphic unit (Bayona et al., 2008a). The lowermost formation is Carbonera that consists of a sandstone unit C3 from a fluvial system, a mudstone unit C2 from a lacustrine system, and a sandstone upper unit C1 (bottom of the studied section), that was accumulated in a fluvial-deltaic system (samples 549.8 to 610.20 m ). Over Carbonera lies the León formation (samples 442.42 to 541.75 m ), a muddy sequence of sediments from a fresh-water lacustrine system. Finally, on top of Carbonera is the Guayabo formation. According to Bayona et al. (2008a) the main


Fig. 1. Geographical setting of the stratigraphic well Saltarín 1A (Llanos Foreland Basin, Colombia).
lithological features of Guayabo's bottom units G1, G2 and G3 that cap the studied section, are:

- G1 (samples from 388.10 to 413.49 m ) and G2 ( 320.08 to 375.33 m ): mostly green-colored laminated mudstones grading to sandstones interbedded with lightcolored massive mudstones with ferruginous nodules. These lithologies are interpreted as the sedimentation from a fluvio-deltaic system changing to a more continental sediment accumulation in fluvial floodplains.
- G3 ( 304.75 to 315.32 m ): mudstones and siltstones accumulated in fluvial flood plains with some evidence of subaerial exposure (light-colored mudstones, formation of ferruginous nodules).

Initial magnetic susceptibility ( $\kappa$ ) was measured at room temperature using a Bartington susceptometer. The $S$-ratio was determined after inducing a high field (ca. 3 T ) and an antiparallel low field (ca. 0.03 T ) IRM. IRMs were measured in a 2 G Enterprises cryogenic magnetometer with a sensitivity of $10^{-11} \mathrm{~A} / \mathrm{m}$.

Table 1. $S$-ratios, $\kappa$ values and corresponding averaged $\delta^{18} \mathrm{O}$ from benthic foraminifera (Zachos et al., 2001) calculated assuming a constant accumulation rate and an age window of 0.005 Ma . Also shown: age constraints and other analyses performed on selected and additional samples (i.e. SEM/EDX, visual analyses of mineral components and high temperature magnetic susceptibility).

| Formation | Unit | Depth [m] | $\kappa[\mathrm{SI}]$ | $S$-ratio | Averaged $\delta^{18} \mathrm{O}[\%]$ | Age Constraints/Analyses |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $\begin{aligned} & 0 \\ & \stackrel{y}{2} \\ & \underset{0}{3} \end{aligned}$ | G3 | 304.75 | 21.84 | 0.58 | 1.33 | Top Middle Miocene |
|  |  | 315.22 | 17.10 | 0.38 | 1.16 | -- |
|  | G2 | 320.08 | 19.53 | 0.09 | 2.26 | Visual Analyses/High $T(\kappa)$ |
|  |  | 329.85 | 14.00 | 0.84 | 1.08 | --- |
|  |  | 351.39 | 27.75 | 0.87 | 1.28 | High $T(\kappa)$ |
|  |  | 355.30 | 23.90 | 0.93 | 1.15 | --- |
|  |  | 360.82 | 23.90 | 0.92 | 1.27 | --- |
|  |  | 370.18 | 25.59 | 0.90 | 1.21 | --- |
|  |  | 375.33 | 21.24 | 0.91 | 1.07 | --- |
|  | G1 | 388.10 | 20.51 | 0.84 | 1.13 | --- |
|  |  | 395.11 | 14.97 | 0.84 | 0.92 | --- |
|  |  | 403.39 | 13.00 | 0.95 | 1.23 | --- |
|  |  | 407.54 | 21.37 | 0.94 | 1.64 | --- |
|  |  | 413.49 | 29.84 | 0.86 | 1.62 | -- |
| $\begin{aligned} & \text { Z } \\ & \text { - } \\ & \hline 1 \end{aligned}$ |  | 442.42 | 24.39 | 0.95 | 1.59 | High $T(\kappa)$ |
|  |  | 444.94 | 25.35 | 0.94 | 1.72 | --- |
|  |  | 447.97 | 23.07 | 0.86 | 1.71 | --- |
|  |  | 450.45 | 19.78 | 0.99 | 1.45 | --- |
|  |  | 453.65 | 19.81 | 0.95 | 1.81 | --- |
|  |  | 458.85 | 22.21 | 0.94 | 1.67 | --- |
|  |  | 462.43 | 46.60 | 0.94 | 1.28 | --- |
|  |  | 475.15 | 22.94 | 0.94 | 1.35 | --- |
|  |  | 479.55 | --- | --- | --- | SEM/EDX |
|  |  | 484.35 | 19.30 | 0.95 | 1.90 | --- |
|  |  | 487.80 | 23.18 | 0.94 | 1.60 | --- |
|  |  | 492.05 | 22.45 | 0.96 | 1.60 | --- |
|  |  | 494.14 | 28.25 | 0.96 | 1.78 | --- |
|  |  | 497.93 | 22.83 | 0.96 | 1.78 | --- |
|  |  | 511.97 | 23.66 | 0.98 | 1.68 | --- |
|  |  | 520.35 | 19.04 | 0.98 | 1.48 | --- |
|  |  | 527.26 | 16.20 | 0.95 | 1.79 | --- |
|  |  | 531.05 | 18.83 | 0.95 | 1.74 | -- |
|  |  | 534.44 | 21.49 | 0.98 | 1.90 | --- |
|  |  | 536.89 | 12.15 | 0.95 | 1.52 | --- |
|  |  | 541.75 | 31.44 | 0.94 | 1.32 | High $T(\kappa)$ |

In the profiles of Fig. 3, global $\delta^{18} \mathrm{O}$ data for benthic foraminifera taken from Zachos et al. (2001), are age-linked to $\kappa$ and $S$-ratios values after assuming a constant accumulation rate for a depth interval flanked by the only two palynological ages available for this stratigraphic well (Carlos Jaramillo, personal communication). These

Table 1. Continuation.

| Formation | Unit | Depth [m] | $\kappa[\mathrm{SI}]$ | $S$-ratio | Averaged $\delta^{18} \mathrm{O}\left[\%{ }^{2}\right]$ | Age Constraints/Analyses |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $$ | C1 | 549.80 | 21.36 | 0.61 | 1.36 | --- |
|  |  | 561.27 | 22.45 | 0.98 | 1.38 | Visual Analyses |
|  |  | 564.50 | 20.28 | 0.96 | 1.51 | --- |
|  |  | 565.14 | 0.00 | 0.83 | 1.52 | --- |
|  |  | 572.35 | 1.93 | 0.96 | 1.10 | --- |
|  |  | 579.24 | 0.00 | 0.93 | 1.48 | --- |
|  |  | 585.10 | 3.63 | 0.85 | 1.93 | --- |
|  |  | 590.94 | 4.85 | 0.92 | 1.95 | --- |
|  |  | 596.16 | 12.27 | 0.95 | 1.43 | --- |
|  |  | 610.20 | 13.93 | 0.97 | 1.77 | Top Lower Miocene |
|  | C2 | 616.48 | --- | --- | --- | High $T$ (к) |
|  | C3 | 669.54 | --- | --- | --- | High $T$ ( $\kappa$ ) |

age constrains are at 305 m (top of the middle Miocene, ca. 11.6 Ma ) and 610 m (top of the lower Miocene, ca. 16 Ma ). The validity of a constant accumulation rate is later revisited in the light of lithostratigraphic evidence and computational results.

The ages of the $\delta^{18} \mathrm{O}$ were calibrated with the geomagnetic polarity time scale of Berggren et al. (1995). The stratigraphic/temporal resolution of this global collection of $\delta^{18} \mathrm{O}$ data is less than $10^{3}$ years for some age intervals. In Zachos et al. (2001), a fivepoint running mean is used to smooth the raw data. An average curve, showing the main tendencies of global ice volume and sea level changes, is adjusted to these points applying a locally weighted mean. Instead of making use of the rough approximation derived from this curve, we have employed an age window of 5 ka (ca 0.35 m ), around the date assigned to each $\kappa$ and $S$-ratio depth level, in order to compute their corresponding average $\delta^{18} \mathrm{O}$ values. Such a window seems to be the optimal one to minimize the standard deviation of averaged $\delta^{18} \mathrm{O}$. Indeed, 5 ka is about a quarter of the shortest (axial precession) Milankovich global climate term. In the depth domain, a precision level of 0.35 m makes sense too, since most of the stratigraphic levels for this well have been given with 2 decimal places of accuracy. Moreover, in the time domain, our sample spacing of about 7 meters corresponds to $10^{5}$ years, the maximum duration of short term aberrant rapid shifts and extreme climate transients (Zachos et al., 1997 and 2001).

We also carried out scanning electron microscopy (SEM) and energy dispersive X-ray spectroscopy (EDX). Only magnetic separates were used for SEM and EDX analyses. These separates were obtained by applying a hand magnet to a suspension in acetone of finely ground rock. Such small amounts of sample were mixed with ethanol and exposed to an ultrasonic bath for approximately 5 minutes. A drop of this preparation was placed on a thin layer of polyethylene set on a carbon holder, and covered by a carbon film ( $\sim 10 \mathrm{~nm}$ ). The scanning electron microscope used for SEM studies was a JEOL JSM6390 and the X-ray probe and energy dispersor was an Oxford Instruments, model 7582.

We show results of some thermomagnetic susceptibility experiments (continuous heating and cooling cycles), performed on selected samples from Guayabo G2/G3


Fig. 2. Schematic lithologic column of the stratigraphic well Saltarin 1A with the limits of the main formations and the corresponding units sampled for this study. Textures and sedimentary structures, as well as stratigraphic breaks (base of channel fill successions) are also shown.
boundary ( 320.08 m ), G2 ( 351.39 m ), G1/León boundary ( 442.42 m ), León/Carbonera boundary ( 541.75 m ). Additionally we show thermomagnetic results for two samples outside the depth interval of this study, namely Carbonera C1/C2 boundary ( 616.48 m ) and Carbonera C3 ( 669.54 m ). For all these experiments, we used a highly sensitive Geofyzika KLY-2 KappaBridge AC Susceptibility meter.

A visual inspection of some ground samples, using a stereomicroscope of 8X to 66X, was also carried out to roughly assess their mineral compositions.

In order to establish a numerical correlation between $\kappa$ or/and $S$-ratio with benthic foraminiferal $\delta^{18} \mathrm{O}$ data, via the inference of $\delta^{18} \mathrm{O}$ values, we used a hybrid Adaptive NeuroFuzzy Inference System (ANFIS) of five layers, that can be interpreted as a neural network with fuzzy parameters or a fuzzy system with distributed parameters. This hybrid NF system is equivalent, under some constrains, to a Takagi-Sugeno-Kang (TSK) model (Finol and Jing, 2002). A TSK system consists of a set of fuzzy if/then rules of the form:

$$
\begin{aligned}
& R_{i} \text { : If } x_{1} \text { is } C_{i 1} \text { and } x_{2} \text { is } C_{i 2} \text { and } \ldots \text { and } x_{n} \text { is } C_{i n}, \\
& \quad \text { Then } y_{i}=c_{i 1} x_{i 1}+c_{i 2} x_{i 2}+\ldots+c_{i n} x_{i n}+c_{i 0}
\end{aligned}
$$



Fig. 3. Profiles of S-ratio and magnetic susceptibility $\kappa$ values between 304.75 m (top Middle Miocene) and 610.20 m (top Lower Miocene) in the stratigraphic well Saltarín 1A. Boundaries between formations (i.e. Guayabo G1, G2 and G3 units and León and Carbonera C1 unit), depth levels corresponding to some selected samples chosen for further detailed analyses and a parallel profile including all global benthic foraminiferal $\delta^{18} \mathrm{O}$ data in $\%$ (after Zachos et al., 2001) are also shown. Profiles of global $\delta^{18} \mathrm{O}$ data for benthic foraminifera are linked to $\kappa$ and $S$-ratios values by assuming a constant accumulation rate for a depth interval flanked by the only two palynological ages available for this well. An age window of 0.005 Ma (ca 0.35 m ) around the date assigned to each $\kappa$ and $S$-ratio depth level is used to compute their corresponding average $\delta^{18} \mathrm{O}$ values (at the upper panel: single crosses connected by a dashed line overimposed to the whole $\delta^{18} \mathrm{O}$ data). This age window minimizes the standard deviation of the averaged $\delta^{18} \mathrm{O}$.

According to the rules above, the output values yi are considered as a linear or constant function of the input variables $x_{j}(j=1,2, \ldots, n) . R_{i}(i=1,2, \ldots, m)$ is the $i$-th fuzzy rule; $C_{i 1}, \ldots, C_{i n}$ are the antecedent linguistic variables and $c_{i 1}, c_{i 2}, \ldots, c_{i n}$ the consequent parameters.

The ANFIS uses these rules and five neural network layers. Each layer has a particular objective (Hurtado et al., 2009):

- The first layer is composed of $n$ membership functions, each implementing a fuzzy decision rule. Its output is the membership function for which the input variable satisfies the associated $C_{i j}$ term.
- The second layer computes every possible combination of the $n$ decision rules. The second layer computes every possible combination of the n decision rules.
- The third layer normalizes the conjunctive membership functions in order to perceive the inputs.
- The fourth layer associates every membership function with an output (the weights are called consequent parameters)
- The last layer combines all the individual outputs to obtain the total output (sums evidences).

To train our fuzzy model we used $S$-ratio or/and $\kappa$ values as input variables and $\delta^{18} \mathrm{O}$ as output variable. We introduced the training data in both, logarithmic and linear forms. In this work, linear, triangular, bell, $\pi$, and gaussian membership functions were tested.

## 3. ROCK MAGNETIC CHARACTERIZATION

High temperature susceptibility curves (heating and cooling), for Guayabo samples at 320.08 m (G2/G3 boundary) and 351.39 m (G2) (Figs. 4 a and b, respectively) appear to have similar behaviors. However, when the scales of these graphs are blown up for a temperature interval between approximately 100 and $400^{\circ} \mathrm{C}$ (insets in Figs. 4a,b), it is possible to identify, only for sample 351.39 m , a small increase of the magnetic susceptibility, around $220^{\circ} \mathrm{C}$. This bump, augmented by a logarithmic scale, probably corresponds to the $\lambda$ transition phase of hexagonal pyrrhotite (Dekkers, 1989). Conversely, such a feature is completely absent in the magnetically weak sample 320.08 m (inset in Fig. 4a). In both cases, the raise of the magnetic susceptibility above $400^{\circ} \mathrm{C}$, accompanied by the major drop around $580^{\circ} \mathrm{C}$, implies that secondary magnetite has been formed upon heating. Magnetite formation, at temperatures above $400^{\circ} \mathrm{C}$, is characteristic of samples like 351.39 m with primary pyrrhotite that irreversibly transforms to magnetite (Dunlop and Özdemir, 1997). Differences in amplitude, for susceptibility changes above $400^{\circ} \mathrm{C}$,


Fig. 4. Magnetic susceptibility curves (heating and cooling) for samples: a) 320.08 m (located on the boundary between Guayabo units G2 and G3) and b) 351.39 m from the unit G2 within the Guayabo formation. The magnetic susceptibility curve for 320.08 m suggests the presence of hematite. The magnetic susceptibility curve for 351.39 m suggests the presence of hexagonal pyrrhotite with a $\lambda$ phase above $220^{\circ} \mathrm{C}$ that is not present in 320.08 m (see insets for both samples).
must be related to the presence of distinct primary magnetic phases for each of these two samples (i.e. hematite for 320.08 m and pyrrotite/magnetite for 351.39 m ). Besides the formation of secondary magnetite, resulting in such large amplitude rises (Figs. 4a,b), the susceptibility signal at 351.39 m might be enhanced by a Hopkinson peak too.

For the specific case of 320.08 m , visual analyses of mineral compositions show some Fe oxides that have been positively identified as hematite. We argue that this mineral is, perhaps, the chief and primary magnetic phase in these rocks since hematite is stable under oxidizing conditions. In fact, the corresponding $S$-ratio value, for this depth level, is the lowest of a well-defined negative anomaly (Fig. 3) that spans between 304.75 and 320.08 m (Guayabo's lower G3 and G2 informal units according to Bayona et al., 2008a). Such an anomaly nearly coincides with a paleoenvironment that includes the presence of oxidized paleosols in G3/G2, between 312.9 to 388 m (Bayona et al., 2008a), and a vastly documented global regression event that occurred at the end of the Serravallian stage (Vail et al., 1977).

Figs. 5a and b show the thermomagnetic curve of sample 442.42 m and the SEM and EDX results for the sample at 479.55 m , both from the León formation. Sample 442.42 m is just at the boundary between the bottom of Guayabo (unit G1) and the top of León. When the temperature scale between 100 and $400^{\circ} \mathrm{C}$ is enlarged, a small rise of the magnetic susceptibility signal, at about $220^{\circ} \mathrm{C}$, is clearly displayed, followed by a drop at around $325^{\circ} \mathrm{C}$ (inset in Fig. 5a). Once more, as in the case of sample at 351.39 m , this feature suggests the presence of pyrrhotite. The increase of the magnetic susceptibility upon heating, above $400^{\circ} \mathrm{C}$, followed by a drop around $580^{\circ} \mathrm{C}$, indicates that magnetite forms in situ and is not a predominant mineral in the original sample.

Sulfur and minute amounts of Fe were also detected, via scanning electron photomicrographs and X-ray energy dispersion spectra, in magnetic separates from sample 479.55 m (Fig. 5b).

The León formation is described as a muddy unit from a fresh-water lacustrine system. It has been extensively reported that, for muddy sediments, accumulated during high water level periods (i.e. warm and humid climate), authigenic formation of magnetic iron sulfides occurs at the very early stages of sedimentation. Fe sulfides form, in these cases, via sulfate reduction and taking advantage of native sulfate and organic carbon (e.g. Sagnotti, 2007; Shouyun et al., 2002; Tric et al., 1991). Accumulation of Fe sulfides is also favored by euxinic lacustrine environments with restricted water circulation, high production of organic matter and relatively high sedimentation rates. The sediments in oxygen depleted bottom waters become rich in organic matter and anoxic because of rapid burial that prevent their oxidation. It seems that, as long as there is a limited amount of sulfide, reactive iron and/or organic matter on hand, iron sulfides such as greigite and pyrrhotite would be preserved with ages that could range from Cretaceous to Holocene (e.g. Babinszki et al, 2007; Otamendi et al., 2006; Weaver et al., 2002, among others). The stability of pyrrhotite is favoured over greigite, in more reducing environments and higher concentrations of $\mathrm{H}_{2} \mathrm{~S}$ (i.e. higher consumption of organic carbon). Since the occurrence of early diagenetic Fe sulfides seems to be produced in muddy lacustrine sediments during interglacial periods, changes of magnetic properties associated to these minerals might be used as environmental proxies (e.g. Babinszki et al., 2007; Mora et al., 2002; Shouyun et al., 2000; Vigliotti et al., 1999; Roberts et al., 1996, among others).

b)


Fig. 5. a) Magnetic susceptibility curve (heating and cooling) for sample 442.42 m at the boundary between Guayabo and León formations. b) SEM photomicrograph and EDX spectra from magnetic separates of sample 479.55 m . Magnetic susceptibility curve for 442.42 m suggests the presence of hexagonal pyrrhotite with a $\lambda$-transition phase above $220^{\circ} \mathrm{C}$ (see inset). SEM and EDX analyses in 479.55 m show the presence of sulfur and minute amounts of Fe .

The upper Carbonera formation (unit C1), characterized by sandstones that have accumulated in a fluvial-deltaic system, represents the bottom of our stratigraphic section. Figs. 6a,b,c show the thermomagnetic curves of samples at 541.75 m (León/Carbonera boundary), 616.48 m (Carbonera C1/C2 boundary) and the lowermost level 669.54 m located in Carbonera unit C3 (these last two samples lying outside our studied section). Again, in all these cases, the presence of hexagonal pyrrhotite seems to be revealed by a $\lambda$ transition phase at about $220^{\circ} \mathrm{C}$ (Dekkers, 1989).

Although Saltarín 1A is a non producer oil well, some impregnations of hydrocarbons have been found in samples from units C 1 and C 2 from the Carbonera formation casting some doubts about the primary or nearly primary origin of Fe-sulfides in these last three samples (Alejandro Mora, personal communication). Indeed, in some settings, Fe-sulfides have also been reported to form during late diagenesis as a consequence of the diffusion
of hydrocarbons and gas through the strata (Reynolds et al., 1994; Thompson and Cameron, 1995; Housen and Mousgrave, 1996).

Visual analyses of mineral components, performed on ground samples from depth level 561.27 m , show the presence of glauconite. Even when this mineral is not magnetic, it is interesting to point out that glauconite is a by-product of early diagenesis and usually forms in shallow waters and mildly reducing environments, during times of slow or negative sediment accumulation. Bayona et al. (2008a) have identified, for the upper Carbonera formation, a number of stratigraphic breaks that are likely related to times of no accumulation and/or erosion. The presence of several channel-fill successions that eroded underlying units (Fig. 2) and the report of glauconite in the upper Carbonera formation indicates that the assumption of a constant sedimentation rate is less valid in


Fig. 6. Magnetic susceptibility curves (heating and cooling) for samples: a) 541.75 m (located on the boundary between León and Carbonera formations); b) 616.48 m (located on the boundary between units C1 and C2 from the Carbonera formation) and c) 669.54 m located at the deepest cored level (unit C3 Carbonera formation). Heating curves in all these three samples suggest the presence of hexagonal pyrrhotite with a $\lambda$ transition phase above $220^{\circ} \mathrm{C}$ (see insets).
this interval rather than in the León and lower Guayabo units.

## 4. COMPUTATIONAL RESULTS

The profiles in Fig. 3 show magnetic parameters ( $S$-ratio and $\kappa$ ), measured at different depth levels in Saltarín 1A, together with their corresponding average benthic foraminiferal $\delta^{18} \mathrm{O}$ values. $S$-ratios and $\kappa$ values are subject to local alteration of the sediments reflecting different sedimentary conditions induced by temperature variations. However, from profiles in Fig. 3 alone, there is not an obvious link between $S$-ratio, $\kappa$ and $\delta^{18} \mathrm{O}$ values.

Fig. 7a,b shows two cross plots for benthic foraminiferal $\delta^{18} \mathrm{O}$ values versus experimental $S$-ratio and $\kappa$ data, respectively. Linear regression analyses in each case, $\delta^{18} \mathrm{O}=-0.1423 S$-ratio $+1.635 \quad\left(R^{2}=0.0068\right) \quad$ and $\quad \delta^{18} \mathrm{O}=-0.0025 \kappa+1.635$ ( $R^{2}=0.0055$ ), prove unsuitable to find out the complex empirical relationships between these two pairs of parameters. These results prompt us to the use of an alternative nonlinear approach (i.e. NFL) to find a family of local fitting functions for different sub groups of experimental data points.

As it was previously indicated, we tested different combinations of these proxies in linear and logarithmic forms, as well as various membership functions. The best results were always accomplished training with the data in linear form and with a Gaussian membership function. Fig. 8 shows the results of our first computational trials by training the net with $S$-ratio and $\delta^{18} \mathrm{O}$ data only. In each case, 2,3 and 4 fuzzy rules (Figs. 8a, b and c , respectively) were employed to monitor a possible improvement of the inference of


Fig. 7. a) Cross plot of experimental S-ratio and global benthic foraminiferal $\delta^{18} \mathrm{O}$ values in $\%$. $S$-ratios are all the 44 data points measured in Saltarín 1A between depth levels 304.75 m (top Mid Miocene) and 610.20 m (top Lower Miocene). Relationship $\delta^{18} \mathrm{O}=-0.1423 S$-ratio +1.635 ( $R^{2}=0.0068$ ) was obtained using a linear regression analysis. b) The same crossplot using $\kappa$ and global benthic foraminiferal $\delta^{18} \mathrm{O}$ values. Relationship $\delta^{18} \mathrm{O}=-0.0025 \kappa+1.635\left(R^{2}=0.0055\right)$ was obtained using a linear regression analysis.
global benthic foraminiferal $\delta^{18} \mathrm{O}$ values. The number of fuzzy rules for the last test (Fig. 8c) is about $10 \%$ of the number of data points we have used to train the NFL system.

To quantify the performance of the fitting, we used the $R^{2}$ correlation between inferred and experimental $\delta^{18} \mathrm{O}$ data, and the Root Mean-Square Error ( $R M S E$ ) values calculated according to:

$$
R M S E=\sqrt{\frac{1}{n} \sum_{i=1}^{n}\left(Y_{i n f}-Y_{\text {exp }}\right)^{2}},
$$

where $Y_{i n f}$ and $Y_{\text {exp }}$ are the inferred and experimental values, respectively, and $n$ is the number of experimental points.

The comparison between $\delta^{18} \mathrm{O}$ inferred values versus global benthic foraminiferal $\delta^{18} \mathrm{O}$ values gave rise to $R^{2}=0.2628$ and $R M S E=0.2468 \%$ using two fuzzy rules, $R^{2}=0.2905$ and $R M S E=0.2421 \%$ using 3 fuzzy rules, and $R^{2}=0.4182$ and


Fig. 8. Benthic foraminiferal $\delta^{18} \mathrm{O}$ inference using an adaptative NeuroFuzzy inference system (ANFIS). These results were obtained by training the NeuroFuzzy system with $100 \%$ of the experimental $S$-ratio values and the benthic foraminiferal $\delta^{18} \mathrm{O}$ data available. Solid lines stand for the inferred data whereas the crosses and dashed lines represent the experimental data. Results of the inference are shown for the three cases: a) 2 fuzzy rules ( $R^{2}=0.2628 ; R M S E=0.2468 \%$ ), b) 3 fuzzy rules $\left(R^{2}=0.2905 ; \quad R M S E=0.2421 \%\right)$ and c) 4 fuzzy rules $\left(R^{2}=0.4182\right.$; $R M S E=0.2222 \%$ ).
$R M S E=0.2222 \%$ using 4 fuzzy rules. The low correlation between inferred and actual data, in these three trials, reveals the inability of the NFL system to predict $\delta^{18} \mathrm{O}$ proxies by training the net with solely $S$-ratio experimental values for Saltarín 1A and global benthic foraminiferal $\delta^{18} \mathrm{O}$ data.

Similar tests were repeated by training the net with $\kappa$ experimental data only and their corresponding benthic foraminiferal $\delta^{18} \mathrm{O}$ values (Fig. 9). $\delta^{18} \mathrm{O}$ inferred values versus global benthic foraminiferal $\delta^{18} \mathrm{O}$ gave rise to $R^{2}=0.0894$ and $R M S E=0.2743 \%$ for two fuzzy rules, $R^{2}=0.1651$ and $R M S E=0.2626 \%$ for three fuzzy rules, and $R^{2}=0.1921$ and $R M S E=0,2584 \%$ for 4 fuzzy rules. Once more, the weak correlation between inferred and actual data show the inability of the NFL system to predict $\delta^{18} \mathrm{O}$ proxies by training the net with $\kappa$ experimental values and global benthic foraminiferal $\delta^{18} \mathrm{O}$ data only.


Fig. 9. Benthic foraminiferal $\delta^{18} \mathrm{O}$ inference using an adaptative NeuroFuzzy inference system (ANFIS). These results were obtained by training the NeuroFuzzy system with $100 \%$ of the experimental magnetic susceptibility ( $\kappa$ ) values and the benthic foraminiferal $\delta^{18} \mathrm{O}$ data available. Solid lines stand for the inferred data whereas the crosses and dashed lines represent the experimental data. Results of the inference are shown for the three cases: a) 2 fuzzy rules $\left(R^{2}=0.08935 ; ~ R M S E=0.2743 \%\right)$, b) 3 fuzzy rules $\left(R^{2}=0.1651 ; ~ R M S E=0.2626 \%\right)$ and c) 4 fuzzy rules ( $R^{2}=0.1921 ; R M S E=0.2584 \%$ ).

As a final trial we trained the NFL system with all the three parameters considered (i.e. $\kappa$ and $S$-ratio as inputs and $\delta^{18} \mathrm{O}$ as output). Since $\kappa$ or $S$-ratios are not related to each other via a simple univocal and linear way (Frank and Nowaczyk 2008; Heslop 2009), we would expect a significant improvement of the inference of $\delta^{18} \mathrm{O}$ data when compared these results with those from the two previous tests.

Fig. 10 shows the results obtained by training the NeuroFuzzy system with $100 \%$ of


Fig. 10. Benthic foraminiferal $\delta^{18} \mathrm{O}$ inference using an adaptative NeuroFuzzy inference system (ANFIS). These results were obtained by training the NeuroFuzzy system with $100 \%$ of the experimental $S$-ratio and $\kappa$ values and the benthic foraminiferal $\delta^{18} \mathrm{O}$ data available. Solid lines stand for the inferred data whereas the crosses and dashed lines represent the experimental data. Results of the inference are shown for the three cases: a) [S-ratio. $\boldsymbol{\kappa}$ ] [12], b) [ $S$-ratio. $\kappa$ ] [21], c) $[S$-ratio. $\kappa][22]$. Accompanying cross plots of inferred $\delta^{18} \mathrm{O}$ versus global benthic foraminiferal $\delta^{18} \mathrm{O}$ are also shown for each test with $R^{2}=0.1586$ and $R M S E=0.2636 \%$ for (a), $R^{2}=0.2975$ and $R M S E=0.2411 \%$ for (b) and $R^{2}=0.6376$ and $R M S E=0.1739 \%$ for (c).

Table 2. Parameters of the Gaussian membership functions [ $\Delta h_{1 / 2}$ Center] and fuzzy rules obtained by training the NFL using $S$-ratio and $\kappa$ data as input variables to infer $\delta^{18} \mathrm{O}$. The $R M S E$ and $R^{2}$ values are also included.

| Membership Functions Parameters |  | Fuzzy Rules | $R M S E[\%]$ | $R^{2}$ |
| :---: | :---: | :---: | :---: | :---: |
| $S$-ratio | $\kappa$ |  |  |  |
| $[0.240-0.113]$ | $[19.786-0.002]$ | $\begin{array}{c}\delta^{18} \mathrm{O}=-24.17(S \text {-ratio }) \\ -0.34 \kappa+18.01 \\ \delta^{18} \mathrm{O}=28.68(S \text {-ratio }) \\ +0.87 \kappa-28.26 \\ {[0.240-0.113]}\end{array}$ | $[19.788-46.597]$ | 0.1739 |$\}$

the $S$-ratio and $\kappa$ experimental values and benthic foraminiferal $\delta^{18} \mathrm{O}$ data available (44 sets of data points). For the first case (Fig. 10a) we considered one membership function for $S$-ratio data and two for $\kappa$ values. This [12] combination gives rise to two fuzzy rules (the product of the number of membership functions of the input variables). The corresponding cross plot of inferred and actual values of $\delta^{18} \mathrm{O}$ reveals a poor inference with a correlation coeficient of $R^{2}=0.1586$ and a $R M S E=0.2636 \%$. We also tried a [2 1] combination of $S$-ratio and $\kappa$ data (i.e. two fuzzy rules, Fig. 10b). Once more, the corresponding cross plot of inferred and actual values of $\delta^{18} \mathrm{O}$ reveals a poor inference with a correlation coeficient of $R^{2}=0.2975$ and a $R M S E=0.2410 \%$. Finally, for the last trial, we used two membership functions for both $S$-ratio and $\kappa$ data ([2 2], four fuzzy rules). The identified TSK model (i.e the membership function values and the four fuzzy rules) are shown in Table 2. As it can be observed in Fig. 10c, a reasonably good correlation was obtained. The $R^{2}(0.6376)$ and $R M S E(0.1739 \%$ ) values in Table 2 confirm this observation. This result seems to indicate a link between magnetic proxies, measured in samples from stratigraphic well Saltarín 1A, and global climate changes mirrored by the variability of benthic foraminiferal $\delta^{18} \mathrm{O}$ data.

Finally we tested how feasible it is the hypothesis of a constant accumulation rate between the two age tie points at 305 and 610 m of depth. We divided the whole interval in 4 subsections of 76.25 m thick each. Two of these subsections, the first and the last, are bond to the first and last ages available. We would expect that the best inference would correspond to the first subsection ( $305 \mathrm{~m} / 381.25 \mathrm{~m}$ ), with a progressive worsening of it as long as we move away from the upper age constraint. We have used the same combination [12] for $S$-ratio and $\kappa$ for each trial illustrated in Figs. 11a,b,c and d. For each cross plot we have obtained: (a) $R^{2}=0.9775, \quad R M S E=0.0502 \%$ (b) $R^{2}=0.7713$, $R M S E=0.08869 \% \quad$ (c) $\quad R^{2}=0.7586, \quad R M S E=0.0673 \% \quad$ and $\quad$ (d) $\quad R^{2}=0.6808$, $R M S E=0.1412 \%$. Notice that the lower correlations correspond to sections b) and d) ( $381.25 \mathrm{~m} / 457.5 \mathrm{~m}$ and $533.75 \mathrm{~m} / 610 \mathrm{~m}$, respectively) that contain some stratigraphic


Fig. 11. The consequences of assuming a constant sedimentation rate between 304.75 m and 610.20 m on the inference of benthic foraminiferal $\delta^{18} \mathrm{O}$ data (in $\%$ ), are assessed by dividing the depth interval in 4 subintervals of about 76.25 m each. The NFL method has been applied in each case using the same combination [ $S$-ratio. $\kappa$ ] [12] for a), b), $\mathbf{c}$ ), and d). Accompanying cross plots of inferred $\delta^{18} \mathrm{O}$ versus global benthic foraminiferal $\delta^{18} \mathrm{O}$ are also shown for each test with $R^{2}=0.9775$ and $R M S E=0.0502 \%$ for (a), $R^{2}=0.7713$ and $R M S E=0.0887 \%$ for (b), $R^{2}=0.7586$ and $R M S E=0.0673 \%$ for (c) and $R^{2}=0.6808$ and $R M S E=0.1412 \%$ for (d).
breaks (Bayona et al., 2008a) probably linked to channel fills. Cross-correlation between magnetic parameters and $\delta^{18} \mathrm{O}$ data would be likely affected by such stratigraphic mismatches at those very subsections. Subsection b has only two of these unconformities whereas subsection d has a total of ten (Fig. 2). As a consequence data dispersion is considerably higher in the latter subsection.

## 5. DISCUSSION AND CONCLUSIONS

The scattering of data points obtained by plotting global benthic foraminiferal $\delta^{18} \mathrm{O}$ values, versus either experimental $S$-ratios (Fig. 7a) or initial magnetic susceptibility $\kappa$
(Fig. 7b), illustrates the impossibility of finding a clean cut relationship between these parameters via traditional methods of linear regression analyses.

The complexities of the problem we are dealing with are most likely related to different factors that could introduce random noise to the magnetic proxies, otherwise directly linked to global climatic changes (i.e. $\delta^{18} \mathrm{O}$ values). Some of these factors are the probable influence of local and regional tectonic events, local climate changes upon sediment composition (Harris and Mix, 2002) and late diagenesis of primary magnetic minerals (Roberts et al., 1996). The hypothesis of a constant accumulation rate, for a 305 m thick stratigraphic sequence in a time period of ca 4.4 Ma , could have also had a consequence upon these results.

Even a non linear approach to this problem, using the hybrid NFL method, requires multiple computational trials to obtain a set of optimal results. We argue that the weak correlation found by training the NFL system with either $\kappa$ or $S$-ratio experimental data and benthic foraminiferal $\delta^{18} \mathrm{O}$ values (Figs. 8 and 9), is because the origin and properties of the various magnetic minerals in these rocks are independently linked, to different extents, to the several factors that preclude a direct connection of their corresponding magnetic parameters to global climatic proxies.

Since $\kappa$ and $S$-ratio experimental values are not related to each other by a simple univocal and linear way (Frank and Nowaczyk, 2008; Heslop, 2009) it is reasonable to believe that an improved inference of the $\delta^{18} \mathrm{O}$ data would be obtained by including both magnetic parameters as input in the training of the NFL system. The optimal fitting gives rise to four fuzzy rules in a combination [22] of $S$-ratio and $\kappa$ data (Fig. 10c). A correlation factor of $R^{2}=0.6376$ and a root mean squared error $\mathrm{RMSE}=0.17389957 \%$ can be interpreted as the result of a major influence (ca. 64\%) of the global climatic changes in the magnetic proxies that we have chosen to infer benthic foraminiferal $\delta^{18} \mathrm{O}$ data.

We argue that the effect of late diagenesis upon primary magnetic minerals is playing a minor role upon these results. Indeed, an advantage of this cored stratigraphic well is that the rocks analyzed are deep enough to have suffered the effects of tardy weathering. The rock magnetic evidence seems to point out to the primary or nearly primary nature of most of the minerals identified in both Guayabo (G1 and G2 units) and León formations. For instante, hematite in G2 appears to be related to a paleoenvironment that includes the presence of oxidized paleosols and a global regression event at the end of the Serravallian stage. Correspondingly, Fe-sulfides (e.g. pyrrhotite) in León might be the by-product of early diagenesis in muddy lacustrine sediments, during times of humid climate, high production of organic matter, slow bottom water circulation and rapid burial of the sediment load.

However, we have also identified Fe -sulfides (e.g. pyrrhotite) in samples from the upper Carbonera sandstone that could be a late diagenesis by-product formed as a consequence of the diffusion of hydrocarbon through these strata. Oil impregnations recognized in these samples support such a presumption. These upper Carbonera strata also coincide with a glauconite-rich region of multiple unconformities or stratigraphic breaks that most likely represent channel fills (Bayona et al., 2008a).

The presence of amalgamated channel-fill successions at the base of the upper unit of the Carbonera formation (Fig. 2), and the record of fluvial-deltaic sediments whose lower
contact shows evidence of stratigraphic breaks (Bayona et al., 2008a), rules out beforehand the validity of assuming a constant accumulation rate for the upper Carbonera unit. In contrast, the rather uniform muddy lithology of the León formation and lower units of the Guayabo formation allows the assumption of a constant accumulation rate.

Therefore, although erroneous for the whole sequence analyzed, the assumption of constant accumulation rate is a good way to independently assess the effectiveness of the NFL method. In fact, after dividing the stratigraphic section in four intervals of equal thickness, and applying the NFL method to infer $\delta^{18} \mathrm{O}$ values in each of them, we find that the lower correlation and major dispersion corresponds to this last subsection. Hydrocarbon induced magnetic phases at these levels could have also contributed to such a mismatch.

From the discussion above it is clear that neither late diagenesis nor the assumption of a constant accumulation rate, appear to be critical factors that have had a significant effect upon the NFL inference over most of the stratigraphic sequence that we have studied here.

Local and regional tectonics and climate changes during early and middle Miocene times, at the Colombian Llanos foreland basin, were the main factors that probably prevented a stronger correlation (i.e. over 64\%) of $S$-ratio and $\kappa$ data to global climatic proxies. The Miocene succession of the Saltarin 1A at the distal segment of the Llanos foreland basin records changes both in tectonic subsidence rates and in composition/location of source areas (Bayona et al., 2008a). The overwhelming increase of tectonic subsidence rates relative to the decrease of supply of sediments, is recorded in the abrupt contact between the upper sandy unit of the Carbonera formation and the muddy León formation. Bayona et al. $(2008 b, 2009)$ interpreted the increase of tectonic subsidence due to the onset of inversion of the whole Eastern Cordillera of Colombia (i.e., flexural subsidence due to orogenic loads) and the effect of large-scale subsidence due to sublithospheric flows associated to the new subduction zone to the west (i.e., dynamic topography subsidence). This change in tectonic conditions also controlled the location of uplifted areas in the distal Llanos basin.

The distal location of uplifted areas due to increasing tectonic subsidence and humid weather favored the flooding of the basin and continue filling with fine-grained terrigenous detritus. Quartzose and subarkosic composition of sandstone beds of the upper unit of the Carbonera formation indicates that sediments were derived from eastward cratonic areas, where intrusive rocks of the Guyana shield crop out. These cratonic regions were totally covered in middle Miocene time by accumulation of the lacustrine sediments of the Leon formation; humid conditions were likely during the time of the Middle Miocene Climatic Optimum. Sandstone beds in the lower Guayabo units document an upsection increase of plagioclase, sedimentary and metamorphic lithic fragments that indicate supply from nearby uplifted blocks located to the south and southeast (Bayona et al. 2008a).

Nevertheless, our novel approach to the assessment of a paleoclimatic problem, applied here to the stratigraphic well Saltarín 1A, shows the scope of the NFL technique in handling geological problems where traditional linear regression methods prove highly limited.

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